
A multicriteria decision model for supplier selection in portfolios with interactions

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Abstract: Supplier evaluation and selection problems are inherently multicriteria decision problems. Numerous analytical techniques ranging from simple weighted scoring to complex mathematical programming approaches have been proposed to solve these problems. However, traditional supplier selection models too often fail to consider the interaction and the capacity interdependency among the suppliers. Suppliers may exhibit internal interactions if the evaluation criteria used for one supplier are believed to be significantly affected by the evaluation criteria used by one or more of the other suppliers in the group. We propose a new branch-and-bound algorithm that generates portfolio alternatives based on Data Envelopment Analysis (DEA). The DEA model proposed in this study evaluates alternative supplier portfolios with a multicriteria model that considers possible interactions among the suppliers.

Keywords: supplier interaction; supply chain management; data envelopment analysis; DEA; supplier selection; multicriteria decision making; MCDM; weighted sum; portfolio modelling.

Reference to this paper should be made as follows: Khakbaz, M.H., Ghapanchi, A.H. and Tavana, M. (2010) 'A multicriteria decision model for supplier selection in portfolios with interactions', *Int. J. Services and Operations Management*, Vol. 7, No. 3, pp.351-377.

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1 Introduction

The rapid evolution of information technology and global competition has drastically increased organisational awareness and responsiveness to customer needs. The constant pressure for customer satisfaction and competitive advantage has forced organisations to search for effective supplier selection strategies (Chou and Chang, 2008). The purpose of supplier selection is to determine the optimal supplier who can offer the best products or services for the customer. Effective supplier evaluation and selection strategies can directly impact supply chain performance resulting in organisational productivity and profitability. Numerous analytical techniques ranging from simple weighted scoring to complex mathematical programming approaches have been proposed to solve these problems. However, traditional supplier selection models too often fail to consider the interaction and the capacity interdependency among the suppliers.

Supplier selection decisions affect various functional areas from procurement of raw materials and components to production and delivery of the end products. The criticality of supplier selection is evident from the significant attention in the literature and its impact on organisational performance (Banker and Khosla, 1995; Dobler *et al.*, 1990; Srinivas *et al.*, 2006). There are four major decisions that are related to the supplier selection problem: What product or services to order, in what quantities, from which suppliers, and in which time periods? There are two kinds of supplier selection situations: single or multiple sourcing. In single sourcing, all the suppliers can fully meet the buyer's price, quantity, quality, and delivery requirements. Consequently, the only decision concerns the selection of the 'best' supplier. In contrast, Multiple sourcing is adopted when either none of the suppliers can satisfy the buyer's total demands or when purchasing strategies aim at avoiding dependency on a single source.

The supplier evaluation and selection literature reports on numerous analytical techniques ranging from simple weighted scoring to complex mathematical programming approaches (Burke *et al.*, 2007; Lee *et al.*, 2001; Maltz and Ellram, 1997; Mishra and Tadikamalla, 2006). The core complexity in these techniques arises from the competing subjective and objective criteria and performance measures (Handfield *et al.*, 2002; Purdy and Safayeni, 2000; Simpson *et al.*, 2002). There can be little dispute that supply chain management has received a great deal of research attention in recent years. Despite the increased interest and attention, most supplier evaluation models consider suppliers as independent entities with no relation or interaction with other entities in the supply chain. The inadequate treatment of supplier interrelationships and interactions with respect to both value and resource utilisation is one of the most important limitations of the present supplier selection research.

We propose a branch-and-bound algorithm that generates alternative portfolios based on Data Envelopment Analysis (DEA). The DEA model proposed in this study evaluates alternative supplier portfolios with a multi-criteria model by considering possible interactions among the suppliers. The primary objective in this study is to consider possible interactions among the suppliers. The model identifies the most influential factors affecting supplier selection decisions and efficiently evaluates a set of alternative portfolios with interactions. The interactions between the suppliers' performance on criteria considered in this paper is a novel approach that has not been studied in the literature. The next section presents literature review followed by a detailed explanation of our mathematical model in Section 3. In Section 4 we describe a case study and in Section 5 we present our conclusions and future research directions.

2 Literature review

Successful supply chain management requires effective sourcing strategies to protect against supply and demand uncertainties. Organisations purchase or outsource products or services from suppliers for reasons such as cost advantage, resource scarcity, insufficient capacity, inadequate time or lack of expertise. Jayaraman *et al.* (1999) show that single sourcing used to determine the best supplier for each purchased part can minimise the total ordering costs. However, this strategy could be detrimental to cost and quality because single suppliers may be dropped for failing to adequately perform their function and their products or services are reassigned to non-optimal

suppliers. They conclude that single sourcing is not the most effective strategy in all cases. Multiple sourcing is a useful strategy to ensure the reliability of a supplier's supply stream. Buyers may purchase or outsource the same products or services from more than one supplier with multiple sourcing. Numerous successful organisations use multiple sourcing to fulfil their requirements and gain competitive advantage (Berger *et al.*, 2004). Hong and Hayya (1992) show multiple sourcing frequently reduces the overall inventory and purchasing costs.

The supplier selection problem requires the consideration of multiple objectives, and hence can be viewed as a Multicriteria Decision Making (MCDM) problem (Bhutta and Huq, 2002). MCDM methods and procedures are commonly used to solve supplier selection problems (Leenders *et al.*, 2006; Monczka *et al.*, 2002; Talluri *et al.*, 2006). Simple weighted rating (Ramanathan, 2007), Analytic Hierarchy Process (AHP) (Akarate *et al.*, 2001; Bhutta and Huq, 2002; Hwang *et al.*, 2005; Muralidharan *et al.*, 2001; Rao, 2007; Sarkis and Talluri, 2002; Tam and Tummala, 2001; Wang *et al.*, 2004), multi-attribute utility theory (Farzipoor Saen, 2007), mathematical programming (Amida *et al.*, 2006), game theory (Dulmin and Mininno, 2003), neural networks (Choy *et al.*, 2002; Choy *et al.*, 2004), goal programming (Araz *et al.*, 2007), decision trees (Berger and Zeng, 2006), neural networks (Ohdar and Ray, 2004), and DEA (Braglia and Petroni, 2000; Joo *et al.*, 2009; Liu *et al.*, 2000; Muralidharan *et al.*, 2002; Weber *et al.*, 1998; Weber *et al.*, 2000) are among the most widely used MCDM methods for supplier evaluation and selection. Narasimhan *et al.* (2001) first used DEA to evaluate the effectiveness of the suppliers. They proposed a methodology where the efficiencies derived from their DEA model were utilised in identifying supplier clusters categorised into high performers and efficient, high performers and inefficient, low performers and efficient, and low performers and inefficient. Other researchers have also studied the application of DEA in supplier selection and negotiating with inefficient suppliers (Weber and Desai, 1996; Weber *et al.*, 1998). Talluri *et al.* (2006) presented a chance-constrained DEA approach in the presence of multiple performance measures that are uncertain. They demonstrated the first application of chance-constrained DEA in the area of purchasing to a previously reported dataset from a pharmaceutical company.

Portfolios of suppliers are commonly suggested as a response to buyer's requirements in multiple sourcing problems (Sarkis and Talluri, 2002; De Boer *et al.*, 1998; Degraeve and Roodhooft, 2000). Portfolio models have their foundation in Markowitz's (2002) pioneering portfolio theory for the management of equity investments. Portfolio models are routinely used in strategic planning and this trend has escalated over the past decade as purchasing management has become more strategic. The AHP is frequently used to evaluate portfolios of suppliers in multiple sourcing (Benyoucef and Canbolat, 2007). Xia and Wu (2007) have proposed an integrated AHP framework improved by rough sets theory and multi-objective mixed integer programming. Their approach considers supplier's capacity constraints and simultaneously determines the number of suppliers and the order quantity allocated to each supplier. Other techniques such as simulation models are also used to assess and compare portfolios of suppliers within a multi-tier sourcing framework (Marquez and Blanchar, 2004).

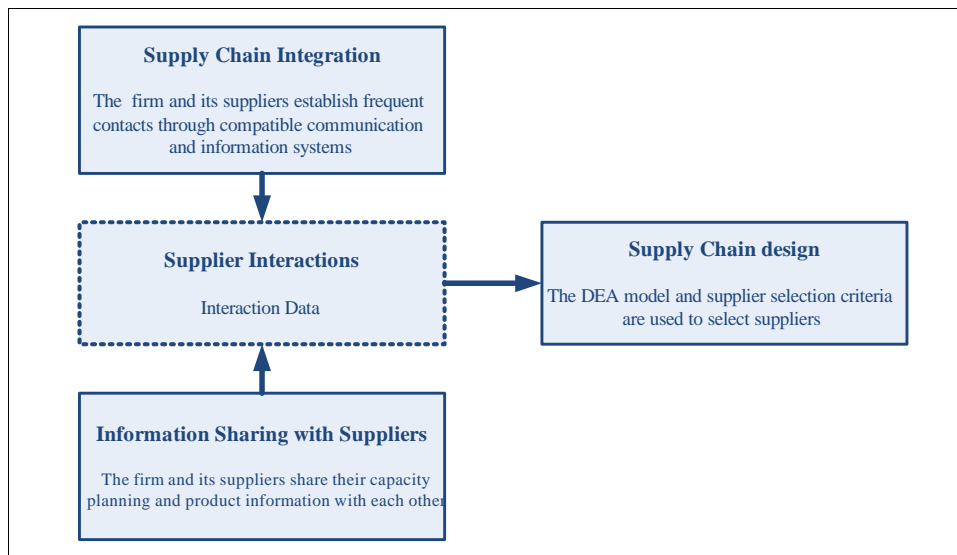
Three key measures used widely for supplier portfolio assessment and selection are price, delivery, and quality (Buffa and Jackson, 1983; Lemke *et al.*, 2000; Pan, 1989). Other measures such as transportation and purchasing costs, vendors' product quality, delivery, and capacity are also proposed for supplier evaluation and selection (Bender *et al.*, 1985; Cavinato, 1992; Merli, 1991). Single versus multiple sourcing preference

orientation of a firm has been shown to have an effect on the supplier selection criteria (Swift, 1995). Swift’s study showed that price and dependability were rated significantly different between those who have a preference for single sourcing and those who have a preference for multiple sourcing. In addition to sourcing preference, other organisational or personal factors have been shown to have an impact on supplier selection criteria.

Effective and efficient design of the supply chain is a powerful competence in improving performance and productivity. Sezen (2008) carried out an empirical study to investigate the relative effects of supply chain integration, information sharing and design on performance. He showed integration, information sharing and specifically supply chain design directly impact flexibility, resource and output performances of supply chains. Sezen (2008) suggested a very useful construct for supply chain design by developing measurements for dependent and independent variables. Dependent variables included flexibility performance, resource performance and output performance. Independent variables included supply chain integration, information sharing with suppliers, information sharing with customers and supply chain design. Some of the measurement scales for integration included the contact frequency among the firms in the supply chain and the compatibility of the information systems. Some of the measurement scales for information sharing included the capacity information sharing among the firm and its suppliers and the ability of the firm to find information about the suppliers’ products and prices.

However, we argue the relative effects of these factors may be more complicated than Sezen (2008) suggests. We show the synergy between integration and information sharing directly impacts supply chain design, *i.e.*, supplier selection. As depicted in Figure 1, this synergy is represented by supplier interaction which in turn results in effective and efficient supply chain design. The effective supply chain design can substantially improve flexibility, resource and output performances of supply chains (Sezen, 2008).

Figure 1 Supplier interactions and supply chain design (see online version for colours)



3 Methodology

We propose a new branch-and-bound algorithm that generates portfolio alternatives based on DEA. The DEA model proposed in this study evaluates alternative supplier portfolios with a multi-criteria model that considers possible interactions among the suppliers.

3.1 The DEA model

DEA is a mathematical programming technique that measures the relative efficiency of multiple Decision-Making Units (DMUs) based on multiple inputs and outputs (Eilat *et al.*, 2006). The number of DMUs is represented by n , each DMU uses m inputs and produces s outputs. Inputs are represented by the vector $X_j = \{x_{ij}\}$ ($i = 1, \dots, m$) and outputs are represented by the vector $Y_j = \{y_{rj}\}$ ($r = 1, \dots, s$) for project j ($j = 1, \dots, n$). The basic DEA model called the Charnes, Cooper and Rhodes (CCR) model was introduced by Charnes *et al.* (1978). In this model, A_0 represents the relative weight of a particular DMU, as the ratio between the weighted-sum of the outputs to the weighted sum of the inputs. The following formulation presents the CCR model where the constant ε is an infinitesimal number that functions as a lower bound for the weights.

$$\text{Max} \quad \frac{\sum_r u_r y_{r0}}{\sum_i v_i x_{i0}} \quad (1)$$

$$\text{s.t.} \quad \frac{\sum_r u_r y_{rj}}{\sum_i v_i x_{ij}} \leq 1 \quad \forall j \quad (2)$$

$$u_r \geq \varepsilon \quad (3)$$

$$v_i \geq \varepsilon. \quad (4)$$

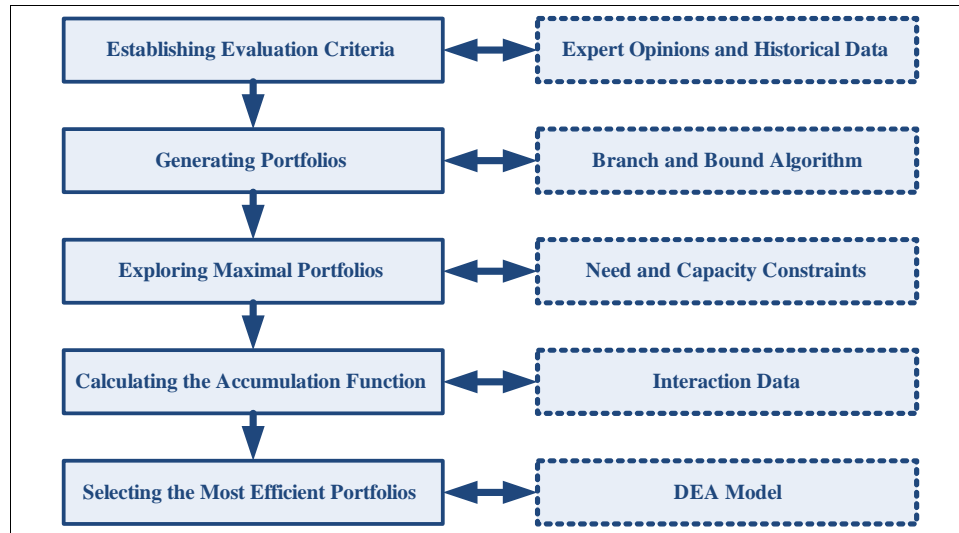
By solving formulation (1) n times (each time evaluating a different DMU), we find the relative efficiency score of the DMUs. These measures divides the DMUs into two categories: efficient DMUs (with score of 1.0) and inefficient DMUs (with scores smaller than 1.0).

3.2 The proposed methodology

The proposed methodology (see Figure 2) is composed of five steps. It begins with the establishment of evaluation criteria through expert opinions and historical data (Step 1). A branch-and-bound model is then applied to generate alternative portfolios and each portfolios' real capacity (the real capacity which the supplier can deliver) and actual capability (the real capacity which the supplier can deliver minus defective products) (Step 2). Subsequently, maximal portfolios are established by considering need and capacity constraints (Step 3). Next, an accumulation function that takes into account the combined effect of possible benefit, outcome, and resource interactions is constructed.

This function is then applied to the capacity, input and outputs of the candidate suppliers in each portfolio to determine aggregate portfolio inputs and outputs (Step 4). Finally, the DEA model is used to determine the most efficient portfolios (Step 5).

Figure 2 The proposed methodology (see online version for colours)



Step 1 Establishing evaluation criteria

In this step, input and output criteria and indices are established by a group of experts. Alternative selection in MCDM is facilitated by evaluating each alternative on the set of criteria. The criterion outcomes provide the basis for comparison of the alternatives under consideration. Therefore, the evaluation criteria must be measurable – even if the measurement is conducted only at the nominal scale. Roy (1996) has argued that criteria in MCDM serve as a basis of a judgement. In this context, the criteria must help establish the preference judgements that form the basis of the decision. Keeney and Raiffa (1976) have suggested that the following five principles be considered when criteria are being selected: completeness (the criteria must embrace all of the essential characteristics of the decision problem), operational ability (the criteria must be meaningful), decomposability (the criteria should be decomposable), non-redundancy (the criteria should avoid duplicate measurement of the same performance), and minimum size (the number of criteria should be manageable and as small as possible). Using these guidelines, we use expert opinions and the firms' data on historical and current proposals to identify the input, outputs, potential capacity for each supplier; and the potential interactions (including input, output, and capacity interactions) between the suppliers.

Step 2 Generating portfolios

This step is intended to generate all possible portfolios using a branch-and-bound technique. The capacity and capability of each portfolio k is also calculated using Equations (5–6). Capacity is the real capacity which the supplier can deliver and capability is the real capacity which the supplier can deliver minus defective products.

$$Capacity_k = \sum_{i=1}^n z_i^k \left(\sum_{j=1}^n z_{ij}^k w_{ij} \right) \quad (5)$$

$$Capability_k = \sum_{i=1}^n z_i^k \left(\sum_{j=1}^n z_{ij}^k w_{ij} \right) \left(\sum_{j=1}^n z_{ij}^k u_{ij}^1 \right). \quad (6)$$

Notations:

- n the total number of suppliers.
- z_i^k the existence of supplier i in portfolio k ($z_i^k = 1$, if supplier i is included in portfolio k ; otherwise, $z_i^k = 0$).
- z_{ij}^k the existence of supplier i and j in portfolio k ($z_{ij}^k = 1$, if both suppliers i and j are included in portfolio k ; otherwise, $z_{ij}^k = 0$).
- w_{jk} the capacity interaction between suppliers j and k (w_{jj} represents the capacity of supplier j).
- v_{jk}^1 the transportation price interaction between suppliers j and k (v_{jj}^1 represents the transportation price of supplier j).
- v_{jk}^2 the product price interaction between suppliers j and k (v_{jj}^2 represents the product price of supplier j).
- u_{jk}^1 the accepted rate interaction between suppliers j and k (u_{jj}^1 represents the accepted rate of supplier j).
- u_{jk}^2 the on-time delivery interaction between suppliers j and k (u_{jj}^2 represents the on-time delivery probability of supplier j).
- u_{jk}^3 the after-sale service quality interaction between suppliers j and k (u_{jj}^3 represents the after-sale service quality of supplier j).
- \hat{x}_k the average amount of input allocated to portfolio k .
- \hat{y}_{rk} the average amount of output r allocated to portfolio k .

Step 3 Exploring maximal portfolios

A portfolio of suppliers is said to be maximal, if the following two conditions hold:

- 1 The portfolio capacity is in the range of our minimum and maximum needs
- 2 Any additional supplier inclusion in the portfolio violates the capacity constraints.

In this step, we model the maximal portfolios as DMUs with specified capacity, input and outputs. To compute the values of capacity, input and outputs for a portfolio as a whole, we use the accumulation function presented in the next step.

Step 4 Calculating the accumulation function

Internal interactions can be further classified into three categories: input interactions, output interactions, and capacity interactions. Input interactions may occur if the total resource requirements of suppliers in the portfolio cannot be represented as the sum of resources of the individual suppliers. This might occur in different situations. For

example, ordering suppliers located in the same geographical location could decrease transportation cost. Also, competition or having a shared board of directors can reduce product price.

Output interactions may occur if the inclusion of two suppliers in a portfolio results in an output which is not equal to the sum of the outputs of the two suppliers. For example, ordering suppliers located in the same geographical location can affect their product accepted rates, delivery times, and after-sale services. Typically, in those cases where suppliers have the same board of directors, they share their capacities to increase their service level and in those cases where the suppliers have the same service provider, their service could potentially decrease. Additionally, competition between suppliers can force them to make higher quality products, and consequently, more accepted rate. Moreover, on-time delivery interactions may occur if the suppliers use the same transportation facilities or have a shared management team that schedules the delivery programme. Usually, having shared transportation facilities can decrease the on-time delivery probability and having a shared management team for a scheduling delivery programme can reduce delivery time.

Capacity interactions may occur if a supplier capacity depends on the other. Generally, if we place an order with two suppliers in the same region, their total capacity could decrease because of the shared and limited resources in the region. Equations (7–10) provide a general accumulation function for all combined input, outputs, and capacity interactions. To account for the input interaction, let v_{ij}^1 and v_{ij}^2 be respectively, the transportation and purchasing price interaction between suppliers i and j . If suppliers i and j are both in a portfolio, v_{ij}^1 and v_{ij}^2 will be added to the transportation and purchasing prices of supplier i . v_{ij}^1 and v_{ij}^2 represent the transportation and purchasing price of supplier j . Similarly, u_{ij}^1 , u_{ij}^2 , and u_{ij}^3 represent the accepted rate, on-time delivery probability, and after-sale service quality level interactions between suppliers i and j . The average amount of input required for portfolio k , is presented by following equation:

$$\hat{x}_k = \frac{\sum_{i=1}^n z_i^k \left(\sum_{j=1}^n z_{ij}^k w_{ij} \right) \left(\sum_{j=1}^n z_{ij}^k (v_{ij}^1 + v_{ij}^2) \right)}{capacity_k} \tag{7}$$

Also, \hat{y}_{rk} , the average amounts of output r allocated to portfolio k , are presented in Equation (10):

$$\hat{y}_{1k} = \frac{capability_k}{capacity_k} \tag{8}$$

$$\hat{y}_{2k} = \frac{\sum_{i=1}^n z_i^k \left(\sum_{j=1}^n z_{ij}^k w_{ij} \right) \left(\sum_{j=1}^n z_{ij}^k u_{ij}^1 \right) \left(\sum_{j=1}^n z_{ij}^k u_{ij}^2 \right)}{capability_k} \tag{9}$$

$$\hat{y}_{3k} = \frac{\sum_{i=1}^n z_i^k \left(\sum_{j=1}^n z_{ij}^k w_{ij} \right) \left(\sum_{j=1}^n z_{ij}^k u_{ij}^1 \right) \left(\sum_{j=1}^n z_{ij}^k u_{ij}^3 \right)}{capability_k} \tag{10}$$

After modelling the portfolios as DMUs, the DEA model is used to find the relative values that reflect the overall attractiveness of the portfolios.

Step 5 Selecting the most efficient portfolios

In this step, the DEA model is applied on maximal portfolios. Each portfolio has an input (\hat{x}_k) and three outputs (\hat{y}_{1k} , \hat{y}_{2k} , and \hat{y}_{3k}). By solving this model n times (each time evaluating a different maximal portfolio), we find the relative efficiency scores of all DMUs. These measures divide the DMUs into two categories: efficient DMUs (with a score of 1.0) and inefficient DMUs (with scores smaller than 1.0).

4 The case study

We use the following case study to illustrate some of the numerical aspects of the proposed methodology. The buyer is Iran Motors Industrial Group,¹ a major Iranian industrial manufacturer. The company manufactures cars for the domestic and export markets. Iran Motors has a long-term relationship with Peugeot Citroën and assembles several Peugeot models under license from the French firm. The company also makes trucks, buses, and passenger cars under license from Mercedes-Benz.

The suppliers are a set of ten steel sheet vendors in four different regions. The demand forecast indicates a need for 2000 to 2200 sheets of steel in the next period. The existing supplier selection models, from linear programming to neural networks, could not be used for portfolio selection because of the high level of interdependency among the suppliers, especially among those located in the same region. While considering supplier interactions adds significantly to the complexity of the model, not considering the interdependencies may result in less than optimal solutions for decision variables such as scheduling of the production line and budget allocation.

Step 1 Establishing evaluation criteria

A group of 15 supply chain management experts from Iran Motors were selected to participate in this study. The Delphi method was utilised to collect and synthesise expert opinions. The Delphi method is based on a structured process for collecting and synthesising knowledge from a group of experts by means of a series of questionnaires combined with controlled opinion feedback (Adler and Ziglio, 1996). The group held several brainstorming sessions to discuss the relevant criteria for selecting suppliers. Several anonymous questionnaires were administered in the form of an iterative consultation procedure. Product price, accepted rate, on-time delivery, and vendor's after-sale service were identified as the four most important factors in evaluating alternative suppliers throughout the Delphi process.

Product price represents the direct purchasing cost of an item on a unit basis. Accepted rate represents the percentage of shipped units that are accepted by the buyer. On-time delivery is measured as the percentage of ordered units that are delivered on-time. After-sale service is the supplier's quality of service to support products. Moreover, the Delphi method identified the total price (purchase price plus transportation cost per unit) as the input factor, and the accepted rate, on-time delivery, and the after-sale service as the output factors. Furthermore, product price was considered as an

input factor because it represent the amount paid by the buyer while accepted rate, on-time delivery, and service performance were considered as output factors because they represented the benefits gained by the buyer. Based on our model convention, higher values of outputs and lower values of inputs are considered desirable. The measures for the accepted rate and on-time delivery are from [0, 1] and after-sale service is measured in terms of a percentage. Although we assumed the three outputs are equal in importance, the model could easily be generalised to consider various weights for each of these factors. The importance weight associated with each factor can be elicited by different weighting procedures. The simplest approach is weighting each factor directly by point allocation. Other weighting methods include SMART and SMARTER (Barron and Barnett, 1996; Edwards and Barron, 1994), SWING (Von Winterfeldt and Edwards, 1986), and AHP (Saaty, 2005). Using SMART, ten points are given to the least important factor. Then, more points are given to the other factors, depending on their relative importance. In SMARTER, the weights are elicited with the centroid method of Solymosi and Dombi (1986). The SWING method is similar, but the procedure starts from the most important factor, keeping it as the reference. In AHP, the weights are derived by comparing all the factors to one another in pairs. Table 1 shows the suppliers data derived from the firms' historical data and proposals.

Table 1 Suppliers and interaction data

| Supplier number | Capacity w_{jk} | Transportation price (dollars) v_{jk}^1 | Product price (dollars) v_{jk}^2 | Accepted rate u_{jk}^1 | On-time delivery u_{jk}^2 | Service u_{jk}^3 |
|-----------------|-------------------|---|------------------------------------|--------------------------|-----------------------------|--------------------|
| 1 | 870 | 92 | 745 | 0.92 | 0.74 | 76.4 |
| 2 | 640 | 74 | 850 | 0.91 | 0.71 | 67.8 |
| 3 | 770 | 97 | 815 | 0.71 | 0.71 | 66.4 |
| 4 | 520 | 113 | 760 | 0.89 | 0.67 | 71.2 |
| 5 | 890 | 102 | 845 | 0.75 | 0.64 | 82.4 |
| 6 | 620 | 69 | 875 | 0.77 | 0.91 | 77.8 |
| 7 | 580 | 76 | 840 | 0.62 | 0.85 | 95.4 |
| 8 | 760 | 89 | 770 | 0.87 | 0.88 | 79.8 |
| 9 | 530 | 92 | 890 | 0.68 | 0.79 | 75.4 |
| 10 | 360 | 105 | 900 | 0.81 | 0.81 | 86.4 |

Next, we illustrate the interactions among the suppliers through capacity, quality, transportation cost, on-time delivery, service performance, and price interdependencies.

Capacity interdependency

The capacity interdependency among the suppliers was noticeably high. For example suppliers 1 and 8 were both located in the Azerbaijan providence in northwestern Iran and used a common source for their raw materials. Selection of both suppliers in a portfolio could potentially decrease their capacity. For example, suppliers 1 and 8 each could supply 870 and 760 units independently. However, when both were selected in the same portfolio, supplier 1 capacity decreased from 870 to 760 ($w_{1,8} = -110$) while supplier 8 capacity decreased from 760 to 670 ($w_{8,1} = -90$) resulting in a total reduction

of 200 units, $w_{1,1} + w_{8,8} - (w_{1,8} + w_{8,1}) = 1430$, or a real capacity of 1090 units considering a 76.23% accepted rate. Similarly, the remaining capacity interactions as well as all the other interaction data are shown in Table 2. A total of 86 portfolios were identified in this study considering supplier interactions but only 77 portfolios met the demand requirement of 2000 to 2200 not considering supplier interactions.

Table 2 Supplier interaction matrix

| Supplier | Supplier | | | | | | | | | |
|----------|---|--|--|--|--|--|--|--|--|--|
| | 1 | 2 | 3 | 4 | 6 | 7 | 8 | 9 | 10 | |
| 1 | | $v_{1,2}^2 = 155$ | | | | | $w_{1,8} = -110$ $v_{1,8}^1 = -7$ $v_{1,8}^2 = 192$ $u_{1,8}^1 = -0.08$ $u_{1,8}^2 = -0.2$ | | | |
| 2 | $v_{2,1}^2 = 55$ | | | $w_{2,4} = -20$ $v_{2,4}^1 = 20$ $u_{2,4}^1 = -0.05$ | | | | | | |
| 3 | | | | $u_{3,4}^3 = 31$ $v_{3,4}^2 = -195$ | | | | | $w_{3,10} = -30$ $v_{3,10}^1 = -5$ $u_{3,10}^1 = -0.04$ $u_{3,10}^2 = +0.1$ | |
| 4 | | $w_{4,2} = -30$ $v_{4,2}^1 = 32$ $u_{4,2}^1 = -0.04$ | $u_{4,3}^3 = 32$ $v_{4,3}^2 = -190$ | | | | | | | |
| 6 | | | | | | $w_{6,7} = -30$ $v_{6,7}^2 = 188$ $u_{6,7}^1 = -0.01$ $u_{6,7}^2 = +0.11$ | | | | |
| 7 | | | | | $w_{7,6} = -20$ $v_{7,6}^2 = 167$ $u_{7,6}^1 = -0.02$ $u_{7,6}^2 = +0.11$ | | | | | |
| 8 | $w_{8,1} = -90$ $v_{8,1}^1 = -10$ $v_{8,1}^2 = 15$ $u_{8,1}^1 = -0.1$ $u_{8,1}^2 = -0.14$ | | | | | | | | | |
| 9 | | | | | | | | | $u_{9,10}^3 = 18$ $v_{9,10}^2 = -188$ | |
| 10 | | | $w_{10,3} = -30$ $v_{10,3}^1 = -5$ $u_{10,3}^1 = -0.05$ $u_{10,3}^2 = +0.1$ | | | | | $u_{10,9}^3 = 19$ $v_{10,9}^2 = -197$ | | |

Consider the requirement of 2000 to 2200 sheets of steel in the next period. There was a possibility that some portfolios supplying over the maximum limit of 2200 units would be omitted from consideration but in reality the actual supply could end up less than this maximum limit because of the interaction among the suppliers. Let us consider the following situation where we first defined all portfolios that supplied between 2000 to 2200 units. Not considering the interaction among the portfolios could have resulted in eliminating portfolios not meeting the minimum requirement. For example, portfolio 0101100001 providing 2004 units could only supply 1909 units because of the interaction between suppliers 2 and 4. We received and paid for $w_{2,2} + w_{4,4} + w_{5,5} + w_{10,10} + w_{2,4} + w_{4,2}$ or 2360 units but we could only use $w_{2,2} \times u_{2,2}^1 + w_{4,4} \times u_{4,4}^1 + w_{5,5} \times u_{5,5}^1 + w_{10,10} \times u_{10,10}^1$ or 2004 units in the production line not considering interactions. However, after considering capacity and quality interactions between suppliers 2 and 4, the real supply was $w'_{2,2} \times u'_{2,2} + w'_{4,4} \times u'_{4,4} + w_{5,5} \times u_{5,5}^1 + w_{10,10} \times u_{10,10}^1$ or 1909 units where $w'_{2,2} = w_{2,2} + w_{2,4} = 620$; $w'_{4,4} = w_{4,4} + w_{4,2} = 490$; $u'_{2,2} = u_{2,2} + u_{2,4} = 0.86$; and $u'_{4,4} = u_{4,4} + u_{4,2} = 0.85$. In contrast, there were other cases where a portfolio did not meet our minimum or maximum requirements and was consequently dropped out of the set but considering the interaction among the suppliers, the portfolio would have met the minimum and maximum requirements. The remaining capacity interactions among the ten suppliers are shown in Table 2. It should be noted that supplier 5 is not in Table 2 because that supplier has no interactions with the other 9 suppliers in the set.

Quality interdependency

Quality interaction represented by the accepted rates (percentage of shipped units that are not rejected) is also an important factor, especially, when suppliers rely on a common source. For example, placing an order with both suppliers 2 and 4 in portfolio 0101100001, reduced the accepted rate of supplier 2 from 0.91 to 0.86 ($u'_{2,2} = u_{2,2} + u_{2,4} = 0.91 - 0.05 = 0.86$) and similarly reduced the accepted rate of supplier 4 from 0.89 to 0.85. Consequently, the average accepted rate dropped from 0.83 to 0.80. Given $u_{2,2}^1 = 0.91$ and $u_{4,4}^1 = 0.89$, the average accepted rate without interaction was $(w'_{2,2} \times u_{2,2}^1 + w'_{4,4} \times u_{4,4}^1 + w_{5,5} \times u_{5,5}^1 + w_{10,10} \times u_{10,10}^1) / W$ or $1959.4 / 2360 = 0.83$; and, given $u'_{2,2} = u_{2,2} + u_{2,4} = 0.91 - 0.05 = 0.86$ and $u'_{4,4} = u_{4,4} + u_{4,2} = 0.89 - 0.04 = 0.85$, the average accepted rate with interaction was $(w'_{2,2} \times u'_{2,2} + w'_{4,4} \times u'_{4,4} + w_{5,5} \times u_{5,5}^1 + w_{10,10} \times u_{10,10}^1) / W$ or 0.80.

Moreover, consider a situation where suppliers in one geographical region purchased their raw materials from the same source. For example suppliers 1 and 8 in northern Iran both purchased their raw iron from the same iron mine. When we placed an order with both suppliers, their combined order put a burden on the supplier of the raw iron which in turn affected the quality of the raw materials and ultimately the quality of the final products (steel sheets). In summary, placing an order with two suppliers might have a downside or upside effect on the capacity and quality. For example, in portfolio 0101100001 where the capacity reduced from 2004 to 1909 and the average accepted rate reduced from 0.83 to 0.80.

Transportation cost interdependency

Transportation cost interdependency also played an important role in the portfolio selection. For example, placing an order with suppliers 2 and 4 separately resulted in a higher transportation cost than placing a joint order with both suppliers. Suppliers 2 and 4 were located in the Zahedan providence in southern Iran where the transportation infrastructure is underdeveloped. Small freight shipment from this region is generally limited and expensive. Placing an order with the two suppliers in this region increased the total transportation cost. The transportation cost per unit for supplier 2 increased by 20 dollars ($v_{2,4}^1 = +20$) from 74 dollars to 94 dollars ($v_{2,2}^1 = v_{2,2}^1 + v_{2,4}^1$) per unit and the transportation cost for supplier 4 increased by 32 dollars ($v_{4,2}^1 = +32$) from 113 dollars to 145 dollars ($v_{4,4}^1 = v_{4,4}^1 + v_{4,2}^1$) per unit. The total transportation cost for portfolio 0111000100 not considering supplier interaction was $w_{2,2}^1 \times v_{2,2}^1 + w_{3,3}^1 \times v_{3,3}^1 + w_{4,4}^1 \times v_{4,4}^1 + w_{8,8}^1 \times v_{8,8}^1 = 243,580$ dollars given $v_{2,2}^1 = 74$ and $v_{4,4}^1 = 113$ while the total cost considering supplier interaction resulted in a total transportation cost of $w_{2,2}^1 \times v_{2,2}^1 + w_{3,3}^1 \times v_{3,3}^1 + w_{4,4}^1 \times v_{4,4}^1 + w_{8,8}^1 \times v_{8,8}^1 = 271,660$ dollars given $v_{2,2}^1 = 74 + 20 = 94$ and $v_{4,4}^1 = 113 + 32 = 145$. On the contrary, it was also possible for the suppliers to combine their shipments and receive volume discount from the freight forwarders. For example, suppliers 1 and 8 were able to combine their shipments and reduce their transportation cost from 92 dollars to 85 dollars per unit for supplier 1 ($v_{1,8}^1 = -7$) and from 89 dollars to 79 dollars per unit for supplier 8 ($v_{8,1}^1 = -10$).

On-time delivery interdependency

Purchasing from suppliers in the same geographical region sometimes resulted in an increase in on-time delivery, especially, when there was a scarcity of resources and lack of manpower in the region. On time delivery is measured as the percentage of ordered units that are not delayed. For example, every time an order was placed with both suppliers 6 and 7 located in the Khorasan providence in northeastern Iran, there was delay in the delivery of the products because both suppliers relied on shared resources and could not fulfil the order in a timely fashion. On the contrary, the interaction among the suppliers sometimes lowered the expected on time delivery. Let us consider portfolio 1100000101 where not considering supplier interaction showed an on-time delivery of $(w_{1,1}^1 \times u_{1,1}^2 + w_{2,2}^1 \times u_{2,2}^2 + w_{8,8}^1 \times u_{8,8}^2 + w_{10,10}^1 \times u_{10,10}^2) / W = 0.81$ where $u_{1,1}^2 = 0.74$, $u_{8,8}^2 = 0.88$, $w_{1,1}^1 = w_{1,1}^1 + w_{1,8}^1 = 760$, and $w_{8,8}^1 = w_{8,8}^1 + w_{8,1}^1 = 770$. However, the real delivery, considering the interaction between suppliers 1 and 8, was $w_{1,1}^1 \times u_{1,1}^2 + w_{2,2}^1 \times u_{2,2}^2 + w_{8,8}^1 \times u_{8,8}^2 + w_{10,10}^1 \times u_{10,10}^2) / W = 0.65$ where $u_{1,1}^2 = u_{1,1}^2 + u_{1,8}^2 = 0.54$, $u_{8,8}^2 = u_{8,8}^2 + u_{8,1}^2 = 0.74$, $w_{1,1}^1 = w_{1,1}^1 + w_{1,8}^1 = 760$, and $w_{8,8}^1 = w_{8,8}^1 + w_{8,1}^1 = 770$.

Service performance interdependency

Service performance, measured using a 1-100 scale, was also affected by the interaction among the suppliers. For example, suppliers 3 and 4 had a contractual agreement to provide after-sale service. Putting both suppliers in the portfolio resulted in an increase in the average after-sales service since both suppliers used a common system for loading, unloading, and identification of the damaged products. For example, the average service performance in portfolio 0111000100 without considering interaction was $(w_{2,2}^1 \times u_{2,2}^3 + w_{3,3}^1 \times u_{3,3}^3 + w_{4,4}^1 \times u_{4,4}^3 + w_{8,8}^1 \times u_{8,8}^3) / W = 70.2$ where $u_{3,3}^3 = 66.4$ and $u_{4,4}^3 = 71.2$ while the average service performance without considering interaction

resulted in an increase in on-time delivery from 70.2 to 84.4 or $(w'_{2,2} \times u_{2,2}^3 + w_{3,3} \times u_{3,3}^3 + w'_{4,4} \times u_{4,4}^3 + w_{8,8} \times u_{8,8}^3) / W$ where $u_{3,3}^3 = u_{3,3}^3 + u_{3,4}^3 = 66.4 + 31 = 97.4$ and $u_{4,4}^3 = u_{4,4}^3 + u_{4,3}^3 = 71.2 + 21 = 92.2$.

Price interdependency

The price interdependency was also noticeable because of the competition among the suppliers. For example, when we placed an order with suppliers 3 and 4, both offered a discounted price and the total cost decreased. In addition, placing an order with two suppliers with unmatchable specifications in the portfolio was also sometimes effective. For example, we used 207 dollars to match products with unmatchable specifications supplied by suppliers 1 and 8 since the steel sheet specifications did not match. Let us consider portfolio 110000101 where the width of two roles coming from suppliers 1 and 8 were not identical. In order to match these roles of steel, we were required to spend 192 dollars on the steel sheets supplied by supplier 1 and 15 dollars on the sheets supplied by supplier 8. The total purchase price without considering interaction was $w'_{1,1} \times v_{1,1}^2 + w_{2,2} \times v_{2,2}^2 + w'_{8,8} \times v_{8,8}^2 + w_{10,10} \times v_{10,10}^2 = 2,027,100$ dollars where $v_{1,1}^2 = 745$ and $v_{8,8}^2 = 770$ whereas considering the interaction between suppliers 1 and 8, the total purchase price was $w'_{1,1} \times v_{1,1}^2 + w_{2,2} \times v_{2,2}^2 + w'_{8,8} \times v_{8,8}^2 + w_{10,10} \times v_{10,10}^2 = 21,845,570$ dollars, where $v_{1,1}^2 = v_{1,1}^2 + v_{1,8}^2 = 937$ and $v_{8,8}^2 = v_{8,8}^2 + v_{8,1}^2 = 770 + 15 = 785$. On the contrary, we considered portfolio 0111000100 where an order placed with both supplier 3 and 4, resulted in a reduced total price of $w'_{2,2} \times v_{2,2}^2 + w_{3,3} \times v_{3,3}^2 + w'_{4,4} \times v_{4,4}^2 + w_{8,8} \times v_{8,8}^2 = 1,716,900$ dollars where $v_{3,3}^2 = v_{3,3}^2 + v_{3,4}^2 = 620$ and $v_{4,4}^2 = v_{4,4}^2 + v_{4,3}^2 = 570$.

Step 2 Generating portfolios

This step generated all possible portfolios using the branch-and-bound technique. The capacity and capability of each portfolio were also calculated using Equations (5–6).

Step 3 Exploring maximal portfolios

All ten steel sheet suppliers in this study had a capability constraint that was more than 2000 and less than 2200 units. In this step, all possible portfolios that met this constraint were identified. The maximal number of portfolios satisfying this constraint was 86, with portfolios including 3 to 6 suppliers.

Step 4 Calculating the accumulation function

In this step, Equations (7–10) were used to calculate the accumulated capacity, input and outputs, taking into account the interactions. As a result for each maximal portfolio four measures were calculated: \hat{x}_k , the average total price allocated to portfolio k ; \hat{y}_{1k} , the accumulated accepted rate allocated to portfolio k ; \hat{y}_{2k} , the accumulated on-time delivery probability allocated to portfolio k ; and, \hat{y}_{3k} , the accumulated after-sale service quality allocated.

Step 5 Selecting the most efficient portfolios

Next, we applied the DEA model to evaluate the portfolios. Each portfolio had an input (\hat{x}_k) and three outputs (\hat{y}_{1k} , \hat{y}_{2k} , and \hat{y}_{3k}). Table 3 presents the sorted portfolios (the top and bottom ten ranked portfolios). For each portfolio, the table gives its identification (a 10-digit binary vector), the corresponding capability, accumulated input and outputs, and the DEA score. These measures divided the portfolios into two categories: those with the score of 1.0 (efficient), and those portfolios with less than a 1.0 score (inefficient).

Table 3 Portfolio evaluation results (sorted DEA scores) (see online version for colours)

| Sorted portfolios | Label | Capacity | Total cost (dollars) | Outputs | | | DEA score |
|-------------------|------------|----------|----------------------|---------------|------------------|--------------------|-----------|
| | | | | Accepted rate | On-time delivery | After-sale service | |
| 1 | 1011000001 | 2010 | 1,940,230 | 0.82 | 0.77 | 92.52 | 1.000000 |
| 2 | 0011001100 | 2030 | 2,091,370 | 0.77 | 0.78 | 95.75 | 0.960115 |
| 3 | 0100010101 | 2013 | 2,191,280 | 0.85 | 0.83 | 77.05 | 0.957329 |
| 4 | 1001010001 | 2032 | 2,129,230 | 0.86 | 0.78 | 77.14 | 0.956381 |
| 5 | 0011010011 | 2047 | 2,153,130 | 0.75 | 0.81 | 96.77 | 0.954045 |
| 6 | 0011010100 | 2148 | 2,145,370 | 0.80 | 0.80 | 91.66 | 0.937279 |
| 7 | 0011000110 | 2031 | 2,080,550 | 0.79 | 0.77 | 91.65 | 0.931810 |
| 8 | 0111000011 | 2057 | 2,148,320 | 0.76 | 0.77 | 94.42 | 0.921667 |
| 9 | 1100000011 | 2035 | 2,201,300 | 0.85 | 0.75 | 82.21 | 0.914675 |
| 10 | 1011001000 | 2170 | 2,166,720 | 0.79 | 0.74 | 94.03 | 0.910080 |
| | | | | | | | |
| 78 | 0010110010 | 2052 | 2,650,810 | 0.73 | 0.75 | 75.68 | 0.710983 |
| 79 | 1000001111 | 2166 | 2,598,580 | 0.75 | 0.73 | 87.69 | 0.707688 |
| 80 | 1010000110 | 2061 | 2,578,300 | 0.76 | 0.69 | 74.22 | 0.695507 |
| 81 | 1010010100 | 2178 | 2,643,120 | 0.77 | 0.72 | 74.79 | 0.694076 |
| 82 | 1010001100 | 2061 | 2,589,120 | 0.74 | 0.70 | 78.41 | 0.682046 |
| 83 | 0110100010 | 2157 | 2,656,890 | 0.76 | 0.70 | 73.43 | 0.681280 |
| 84 | 0110101000 | 2156 | 2,667,710 | 0.75 | 0.72 | 77.50 | 0.677650 |
| 85 | 0010111001 | 2199 | 3,126,770 | 0.71 | 0.84 | 80.49 | 0.676796 |
| 86 | 1000100110 | 2182 | 2,718,890 | 0.77 | 0.66 | 78.89 | 0.668796 |
| 87 | 1000101100 | 2181 | 2,729,710 | 0.75 | 0.68 | 82.83 | 0.654420 |

In this case study, we identified one portfolio with the score of 1.0, and 4 portfolios with a score higher than 0.95 (see Table 3). The top portfolio is 1011000001 with suppliers 1, 3, 4, and 10. Our study revealed that the analysis does not point out a single best portfolio. Rather, it reduces the large number of potential portfolios significantly to a small and manageable number of attractive alternative choices, while integrating several seemingly different criteria. To show the importance of the interaction among the suppliers, we ran our model again without interaction consideration. The results are presented in Table 4.

Table 4 Portfolio evaluation results (without interactions) (see online version for colours)

| Sorted portfolios | Label | Capacity | Total cost (dollars) | Outputs | | | DEA score |
|-------------------|------------|----------|----------------------|---------------|------------------|--------------------|-----------|
| | | | | Accepted rate | On-time delivery | After-sale service | |
| 1 | 1100000100 | 2044 | 1,972,390 | 0.90 | 0.78 | 75.11 | 1.000000 |
| 2 | 0100010101 | 2013 | 2,191,280 | 0.85 | 0.83 | 77.05 | 0.961508 |
| 3 | 1000001101 | 2113 | 2,274,110 | 0.82 | 0.82 | 83.09 | 0.959473 |
| 4 | 1001010001 | 2032 | 2,129,230 | 0.86 | 0.78 | 77.14 | 0.951383 |
| 5 | 1100001001 | 2034 | 2,212,630 | 0.83 | 0.77 | 80.12 | 0.950847 |
| 6 | 1010000100 | 2008 | 2,083,270 | 0.84 | 0.77 | 74.27 | 0.942269 |
| 7 | 1000100100 | 2129 | 2,223,860 | 0.84 | 0.75 | 79.54 | 0.939239 |
| 8 | 1100100000 | 2050 | 2,162,380 | 0.85 | 0.69 | 76.33 | 0.926929 |
| 9 | 0101001100 | 2066 | 2,229,440 | 0.83 | 0.79 | 78.56 | 0.925275 |
| 10 | 1101000001 | 2137 | 2,135,310 | 0.89 | 0.73 | 74.47 | 0.917327 |
| | | | | | | | |

A comparison between Tables 3 and 4 shows that portfolio 1000010100 with a supply of 2063 units can only produce 1632 units, portfolio 1001000100 with a supply of 2054 units can only produce 1617 units, and portfolio 1100000100 with 1737 units can only produce 1617 units all due to the interaction among the suppliers. A closer examination of the results further shows very little consistency among the top ten portfolios in the two lists presented in Tables 3 and 4. For example, the portfolio 1011000001 with a total cost of 1,940,230 dollars and a DEA score of 1.00 in Table 3 is not among the top 10 portfolios in Table 4. Similarly, the portfolios 0011001100, 0011010011, 0011010100, 0011000110, 0111000011, 1100000011, and 1011001000 do not appear among the top 10 portfolios in Table 4. Only 2 portfolios appear on both lists: portfolios 0100010101 with total cost of 2,191,280 dollars and portfolio 1001010001 with total cost of 2,129,230 dollars. The 2 portfolios appear on both lists because there is no interaction between suppliers 2, 6, 8 and 10; and between suppliers 1, 4, 6 and 10 (see Table 2). We should note the cost of modelling and obtaining all the data for every possible interaction is not included in the overall cost benefit assessment. However, in cases where this information is readily available or quantifiable, it should be considered in the cost function.

A sensitivity analysis was performed on the interaction categories to see how sensitive the rankings of the various portfolios were to $\pm 5\%$ and $\pm 10\%$ changes in the parameters. For example, the initial capacity values were changed by $\pm 5\%$ and the resulting rankings were compared to see the overall impact these changes had on the final decision. The results for the top five candidates from the list of eligible portfolios are given in Table 5. Notice that when the capacity was increased by 5%, only portfolios 1011000001 and 0011001100 remained on the top-5 list and when the capacity was decreased by 5%, the top 5 portfolios were different. We also performed a sensitivity analysis with $\pm 10\%$ on the capacity. When the capacity was increased by 10%, the top five portfolios were different from the top five portfolios when the capacity was reduced by 10%. Similarly, a 5% increase in the accepted rate produced different portfolios for

the top five compared with a 5% reduction in the accepted rate. Thus, the rankings were quite sensitive to small changes in the capacity and the accepted rate. Table 5 presents the partial results from the sensitivity analysis.

Table 5 Sensitivity analysis results (see online version for colours)

| Interaction category | Sensitivity range | Number of eligible portfolios | Portfolio labels | Capacity | Total cost (dollars) | Outputs | | | DEA score |
|----------------------|-----------------------|-------------------------------|------------------|----------|----------------------|---------------|------------------|--------------------|-----------|
| | | | | | | Accepted rate | On-time delivery | After-sale service | |
| Capacity | Capacity +5% | 79 | 0011001011 | 2028 | 2,206,359 | 0.71 | 0.80 | 100.83 | 1.000000 |
| | | | 1000010011 | 2026 | 2,126,429 | 0.81 | 0.81 | 84.94 | 1.000000 |
| | | | 1001000011 | 2011 | 1,988,543 | 0.84 | 0.75 | 83.74 | 1.000000 |
| | | | 1011000001 | 2112 | 2,039,810 | 0.82 | 0.77 | 92.53 | 1.000000 |
| | | | 0011001100 | 2132 | 2,195,939 | 0.77 | 0.78 | 95.75 | 0.958525 |
| | Capacity -5% | 96 | 0011000111 | 2117 | 2,107,383 | 0.77 | 0.81 | 96.36 | 1.000000 |
| | | | 0011010100 | 2041 | 2,038,102 | 0.80 | 0.80 | 91.66 | 1.000000 |
| | | | 0111000100 | 2048 | 2,031,516 | 0.82 | 0.75 | 89.19 | 1.000000 |
| | | | 1011001000 | 2061 | 2,058,384 | 0.79 | 0.74 | 94.03 | 1.000000 |
| | | | 1011000010 | 2062 | 2,048,105 | 0.81 | 0.73 | 90.06 | 0.988968 |
| Accepted rate | Accepted rate +5% | 80 | 0011001011 | 2028 | 2,099,130 | 0.75 | 0.80 | 100.83 | 1.000000 |
| | | | 1000010011 | 2026 | 2,025,170 | 0.85 | 0.81 | 84.94 | 1.000000 |
| | | | 1001000011 | 2011 | 1,893,850 | 0.88 | 0.75 | 83.74 | 1.000000 |
| | | | 1011000001 | 2113 | 1,940,230 | 0.86 | 0.77 | 92.52 | 1.000000 |
| | | | 0101000101 | 2000 | 2,043,370 | 0.90 | 0.78 | 75.64 | 0.960386 |
| | Accepted rate -5% | 97 | 0011000111 | 2117 | 2,220,690 | 0.74 | 0.81 | 96.37 | 1.000000 |
| | | | 0011010100 | 2041 | 2,145,370 | 0.76 | 0.80 | 91.66 | 1.000000 |
| | | | 0111000100 | 2047 | 2,140,560 | 0.78 | 0.75 | 89.19 | 1.000000 |
| | | | 1011001000 | 2061 | 2,166,720 | 0.75 | 0.74 | 94.03 | 1.000000 |
| | | | 1011000010 | 2062 | 2,155,900 | 0.77 | 0.73 | 90.06 | 0.989774 |
| On-time delivery | On-time delivery +10% | 87 | 1011000001 | 2010 | 1,940,230 | 0.82 | 0.84 | 92.52 | 1.000000 |
| | | | 0100010101 | 2013 | 2,191,280 | 0.85 | 0.91 | 77.05 | 0.962276 |
| | | | 0011001100 | 2030 | 2,091,370 | 0.77 | 0.86 | 95.75 | 0.960115 |
| | | | 1001010001 | 2032 | 2,129,230 | 0.86 | 0.86 | 77.14 | 0.956381 |
| | | | 0011010011 | 2047 | 2,153,130 | 0.75 | 0.89 | 96.77 | 0.954795 |
| | On-time delivery -10% | 87 | 1011000001 | 2010 | 1,940,230 | 0.82 | 0.70 | 92.52 | 1.000000 |
| | | | 0011001100 | 2030 | 2,091,370 | 0.77 | 0.70 | 95.75 | 0.960115 |
| | | | 1001010001 | 2032 | 2,129,230 | 0.86 | 0.70 | 77.14 | 0.956381 |
| | | | 0011010011 | 2047 | 2,153,130 | 0.75 | 0.74 | 96.77 | 0.953140 |
| | | | 0100010101 | 2013 | 2,191,280 | 0.85 | 0.75 | 77.05 | 0.951350 |

Table 5 Sensitivity analysis results (see online version for colours) (continued)

| Interaction category | Sensitivity range | Number of eligible portfolios | Portfolio labels | Capacity | Total cost (dollars) | Outputs | | | DEA score |
|----------------------|---------------------------|-------------------------------|------------------|----------|----------------------|---------------|------------------|--------------------|-----------|
| | | | | | | Accepted rate | On-time delivery | After-sale service | |
| Service performance | Service Performance +5% | 87 | 1011000001 | 2010 | 1,940,230 | 0.82 | 0.77 | 91.08 | 1.000000 |
| | | | 0011001100 | 2030 | 2,091,370 | 0.77 | 0.78 | 94.73 | 0.964865 |
| | | | 0100010101 | 2013 | 2,191,280 | 0.85 | 0.83 | 80.90 | 0.957329 |
| | | | 1001010001 | 2032 | 2,129,230 | 0.86 | 0.78 | 81.00 | 0.956381 |
| | | | 0011010011 | 2047 | 2,153,130 | 0.75 | 0.81 | 95.87 | 0.954045 |
| | Service Performance -5% | 87 | 1011000001 | 2010 | 1,940,230 | 0.82 | 0.77 | 85.16 | 1.000000 |
| | | | 0011001100 | 2030 | 2,091,370 | 0.77 | 0.78 | 87.99 | 0.958576 |
| | | | 0100010101 | 2013 | 2,191,280 | 0.85 | 0.83 | 69.35 | 0.957329 |
| | | | 1001010001 | 2032 | 2,129,230 | 0.86 | 0.78 | 69.43 | 0.956381 |
| | | | 0011010011 | 2047 | 2,153,130 | 0.75 | 0.81 | 89.36 | 0.954045 |
| Transportation Price | Transportation Price +10% | 87 | 1011000001 | 2010 | 1,964,753 | 0.82 | 0.77 | 92.52 | 1.000000 |
| | | | 0011001100 | 2030 | 2,115,887 | 0.77 | 0.78 | 95.75 | 0.960984 |
| | | | 0100010101 | 2013 | 2,210,838 | 0.85 | 0.83 | 77.05 | 0.960853 |
| | | | 1001010001 | 2032 | 2,151,168 | 0.86 | 0.78 | 77.14 | 0.958592 |
| | | | 0011010011 | 2047 | 2,178,803 | 0.75 | 0.81 | 96.77 | 0.954720 |
| | Transportation Price -10% | 87 | 1011000001 | 2010 | 1,915,707 | 0.82 | 0.77 | 92.52 | 1.000000 |
| | | | 0011001100 | 2030 | 2,066,853 | 0.77 | 0.78 | 95.75 | 0.959225 |
| | | | 1001010001 | 2032 | 2,107,292 | 0.86 | 0.78 | 77.14 | 0.954124 |
| | | | 0100010101 | 2013 | 2,171,722 | 0.85 | 0.83 | 77.05 | 0.953741 |
| | | | 0011010011 | 2047 | 2,127,457 | 0.75 | 0.81 | 96.77 | 0.953354 |
| Price | Price +10% | 87 | 1011000001 | 2010 | 2,134,575 | 0.82 | 0.77 | 92.52 | 1.000000 |
| | | | 1001010001 | 2032 | 2,320,215 | 0.86 | 0.78 | 77.14 | 0.965570 |
| | | | 0100010101 | 2013 | 2,390,850 | 0.85 | 0.83 | 77.05 | 0.965306 |
| | | | 0011001100 | 2030 | 2,300,885 | 0.77 | 0.78 | 95.75 | 0.960102 |
| | | | 0011010011 | 2047 | 2,384,080 | 0.75 | 0.81 | 96.77 | 0.947931 |
| | Price -10% | 87 | 1011000001 | 2010 | 1,745,885 | 0.82 | 0.77 | 92.52 | 1.000000 |
| | | | 0011010011 | 2047 | 1,922,180 | 0.75 | 0.81 | 96.77 | 0.961629 |
| | | | 0011001100 | 2030 | 1,881,855 | 0.77 | 0.78 | 95.75 | 0.960130 |
| | | | 0100010101 | 2013 | 1,991,710 | 0.85 | 0.83 | 77.05 | 0.947753 |
| | | | 1001010001 | 2032 | 1,938,245 | 0.86 | 0.78 | 77.14 | 0.945382 |

On the other hand, the rankings were somewhat insensitive to small changes in the on-time delivery, the service performance, the transportation price and the total price. For example, a $\pm 10\%$ change in the on-time delivery produced the same portfolios in the top five with only a few changes in the relative rankings of these five portfolios.

Table 6 Supplier interaction matrix (considering interaction between suppliers 7 and 9)

| Supplier | Supplier | | | | | | | | |
|----------|---|--|--|--|--|--|--|--|--|
| | 1 | 2 | 3 | 4 | 6 | 7 | 8 | 9 | 10 |
| 1 | | $v_{1,2}^2 = 155$ | | | | | $w_{1,8} = -110$ $v_{1,8}^1 = -7$ $v_{1,8}^2 = 192$ $u_{1,8}^1 = -0.08$ $u_{1,8}^2 = -0.2$ | | |
| 2 | $v_{2,1}^2 = 55$ | | | $w_{2,4} = -20$ $v_{2,4}^2 = 20$ $u_{2,4}^1 = -0.05$ | | | | | |
| 3 | | | | $u_{3,4}^3 = 31$ $v_{3,4}^2 = -195$ | | | | | $w_{3,10} = -30$ $v_{3,10}^1 = -5$ $u_{3,10}^1 = -0.04$ $u_{3,10}^2 = +0.1$ |
| 4 | | $w_{4,2} = -30$ $v_{4,2}^1 = 32$ $u_{4,2}^1 = -0.04$ | | $u_{3,4}^3 = 32$ $v_{3,4}^2 = -190$ | | | | | |
| 6 | | | | | | $w_{6,7} = -30$ $v_{6,7}^2 = 188$ $u_{6,7}^1 = -0.01$ $u_{6,7}^2 = +0.11$ | | | |
| 7 | | | | | $w_{7,6} = -20$ $v_{7,6}^2 = 167$ $u_{7,6}^1 = -0.02$ $u_{7,6}^2 = +0.11$ | | | $u_{7,9}^1 = +0.06$ $v_{7,9}^2 = 0.0$ | |
| 8 | $w_{8,1} = -90$ $v_{8,1}^1 = -10$ $v_{8,1}^2 = 15$ $u_{8,1}^1 = -0.1$ $u_{8,1}^2 = -0.14$ | | | | | | | | |
| 9 | | | | | | | $u_{9,7}^1 = 0.0$ $v_{9,7}^2 = -89$ | | $u_{9,10}^3 = 18$ $v_{9,10}^2 = -188$ |
| 10 | | | $w_{10,3} = -30$ $v_{10,3}^1 = -5$ $u_{10,3}^1 = -0.05$ $u_{10,3}^2 = +0.1$ | | | | | $u_{10,9}^3 = 19$ $v_{10,9}^2 = -197$ | |

Table 7 Portfolio evaluation results (considering interaction between suppliers 7 and 9) (see online version for colours)

| Sorted portfolios | Label | Capacity | Total cost (dollars) | Outputs | | | DEA score |
|-----------------------------|------------|----------|----------------------|---------------|------------------|--------------------|-----------|
| | | | | Accepted rate | On-time delivery | After-sale service | |
| 1 | 1011000001 | 2010 | 1,940,230 | 0.82 | 0.77 | 92.52 | 1.000000 |
| 2 | 0011001100 | 2030 | 2,091,370 | 0.77 | 0.78 | 95.75 | 0.960115 |
| 3 | 0100010101 | 2013 | 2,191,280 | 0.85 | 0.83 | 77.05 | 0.957329 |
| 4 | 1001010001 | 2032 | 2,129,230 | 0.86 | 0.78 | 77.14 | 0.956381 |
| 5 | 0011010011 | 2047 | 2,153,130 | 0.75 | 0.81 | 96.77 | 0.954045 |
| 6 | 0011010100 | 2148 | 2,145,370 | 0.80 | 0.80 | 91.66 | 0.937279 |
| 7 | 0011000110 | 2031 | 2,080,550 | 0.79 | 0.77 | 91.65 | 0.931810 |
| 8 | 0111000011 | 2057 | 2,148,320 | 0.76 | 0.77 | 94.42 | 0.921667 |
| 9 | 1100000011 | 2035 | 2,201,300 | 0.85 | 0.75 | 82.21 | 0.914675 |
| 10 | 1011001000 | 2170 | 2,166,720 | 0.79 | 0.74 | 94.03 | 0.910080 |
| | | | | | | | |
| 29 (With interaction) | 1001001010 | 2018 | 2,281,060 | 0.81 | 0.76 | 79.51 | 0.842282 |
| 29 (Without interaction) | 1001001010 | 1983 | 2,233,890 | 0.79 | 0.76 | 79.51 | |
| | | | | | | | |
| 78 | 0010110010 | 2052 | 2,650,810 | 0.73 | 0.75 | 75.68 | 0.710983 |
| 79 | 1000001111 | 2166 | 2,598,580 | 0.75 | 0.73 | 87.69 | 0.707688 |
| 80 | 1010000110 | 2061 | 2,578,300 | 0.76 | 0.69 | 74.22 | 0.695507 |
| 81 | 1010010100 | 2178 | 2,643,120 | 0.77 | 0.72 | 74.79 | 0.694076 |
| 82 | 1010001100 | 2061 | 2,589,120 | 0.74 | 0.70 | 78.41 | 0.682046 |
| 83 | 0110100010 | 2157 | 2,656,890 | 0.76 | 0.70 | 73.43 | 0.681280 |
| 84 | 0110101000 | 2156 | 2,667,710 | 0.75 | 0.72 | 77.50 | 0.677650 |
| 85 | 0010111001 | 2199 | 3,126,770 | 0.71 | 0.84 | 80.49 | 0.676796 |
| 86 | 1000100110 | 2182 | 2,718,890 | 0.77 | 0.66 | 78.89 | 0.668796 |
| 87 | 1000101100 | 2181 | 2,729,710 | 0.75 | 0.68 | 82.83 | 0.654420 |

In addition to the interaction on the suppliers' performance on one particular criterion, we also considered interactions in performance on multiple criteria. For example, we considered a scenario where there was a price competition and price reduction when two suppliers were in the portfolio, one reduced price, while the other increased quality as competitive reaction because that was the aspect on which they could easily compete. We considered a situation where there was a competition between suppliers 7 and 9. When an order was placed with both suppliers, supplier 9 reduced its price by

10% ($u_{7,9}^1 = +0.06$, $v_{7,9}^2 = 0.0$ and $u_{9,7}^1 = 0.0$, $v_{9,7}^2 = -89$) and in reaction, supplier 7 increased quality by 10% (see Table 6). For example, the accepted rate of supplier 7 in portfolio 1001001010 was increased from 0.62 to 0.68. This change produced an eligible portfolio to be entered in the DEA model. Given $u_{7,7}^1 = 0.62$ and $u_{9,7}^1 = 0.0$, the average accepted rate without interaction was $(w_{1,1} \times u_{1,1}^1 + w_{4,4} \times u_{4,4}^1 + w_{7,7} \times u_{7,7}^1 + w_{9,9} \times u_{9,9}^1) / W = 0.79$; and, given $u_{7,7}^{1'} = u_{7,7}^1 + u_{7,9}^1 = 0.62 + 0.06 = 0.68$, the average accepted rate with interaction was $(w_{1,1} \times u_{1,1}^1 + w_{4,4} \times u_{4,4}^1 + w_{7,7} \times u_{7,7}^{1'} + w_{9,9} \times u_{9,9}^1) / W = 0.81$. The complete results considering the price and quality interaction between suppliers 7 and 9 are presented in Table 7. In summary, our model cannot only deal with the interaction on the suppliers' performance on one particular criterion, it can also deal with performance on multiple criteria.

5 Conclusions and future research directions

Supplier portfolio selection is one of the most important activities of purchasing managers in which cost, quality, delivery, service, and other competing factors should be considered in selecting the most attractive portfolios. Shortage of suppliers' capacity and the accepted rate make the problem difficult to formulate and solve. Furthermore, considering interactions between the suppliers makes the problem more complicated. We used a branch-and-bound algorithm that generated portfolio alternatives based on DEA. The DEA model developed in this study evaluated alternative supplier portfolios with a multi-criteria model that considered possible interactions among the suppliers. Although interactions assumed in this paper are simplified, in reality, they could be quite complex. This consideration of interactions can open a new discussion that could improve the existing supplier selection literature.

The model has a number of advantages:

- 1 It considers multiple criteria such as capacity, transportation and purchasing costs, quality, delivery, and after-sale service in supplier selection problems.
- 2 It considers interaction of capacity, transportation and purchasing costs, quality, delivery, and after-sale service between suppliers.
- 3 It considers the total cost of purchasing rather than unit price of the product. The total cost function also considers both transportation and purchasing costs.
- 4 It considers allocation of the order quantities for multiple sourcing with constraints.
- 5 It can be solved using the user-friendly and easy to use Solver capabilities of Microsoft Excel.

The consideration of multiple criteria, total cost rather than purchase price, order allocation, and user-friendliness are issues that have been considered in the supplier selection literature. However, the interactions between the suppliers' performance on criteria considered in this paper is a novel approach that has not been studied in the literature. Although our model deals with multiple sourcing problems, further research is needed to study the effects of supplier interactions on other sourcing strategies such as parallel sourcing, network sourcing and hybrid sourcing.

The numerical example presented in this paper shows the effect of our model on supply chain performance. The comparison between the results using interactions versus no interactions show there are significant differences in the rankings of the portfolios as well as significant differences in the total cost and the output measures. Failure to consider supplier interactions may lead to poor supplier choices. This result is also confirmed from the sensitivity analysis which shows the rankings of the portfolios are quite sensitive both to the accepted rate and the capacity. Although we have only carried out a numerical example for a specific case, the revealing results point to the need for further research on supplier interactions. It should be noted that much of the current research on supplier evaluation and selection is quantitative. The numerical results provided by our model and other similar models in supplier selection and evaluation should be used to study the qualitative aspects of supplier selection decisions.

The model proposed in this study promotes integration and information sharing. Suppliers view information sharing as attractive and are intently focused on upgrading their information-sharing capabilities in supply chains (Fawcett *et al.*, 2007; Zhou and Benton, 2007). However, integration and information sharing initiatives are poorly scoped and groundwork for success is rarely established. The bridges to integration and information sharing are not built on solid ground and neither the structure nor the culture needed to share information is established. The information sharing challenge is exacerbated by organisational cultures that reduce suppliers' willingness to share the information needed to improve overall supply chain performance. Willingness as a key to information sharing is often overlooked receives little managerial attention. This must change if supply chains are to obtain the 'full' return on their integration and information sharing initiatives.

The literature review suggests much of the emphasis on supplier evaluation and selection process has been given to the decision criteria and the decision making methods. More research is needed on the design and development of appropriate methods for obtaining the interaction data. These methods could address questions such as 'how could we collect all the necessary information?', 'how willing are the suppliers in providing this data?' or 'how reliable are the collected data?' Another area for future research is to model the communication process between the buyer and the suppliers as an electronic reverse auction where there is a dynamic flow of information between the buyer and the suppliers. Clearly there are a host of interesting questions related to the information gathering and the implementation phases in our model. In addition, more research is needed to examine the qualitative and non-quantitative aspects of supplier selection process. However, the problem of quantifying qualitative factors remains a difficult task in supplier evaluation and selection research.

The fast development and deep penetration of information technologies and internet have given rise to the proliferation of electronic mechanisms for inter-organisational exchange. Inter-organisational exchange deals with transactions between the firm and the suppliers (and between the suppliers) in a supply chain. The framework proposed in this study can be deployed through diverse forms of electronic inter-organisational systems ranging from simple information links to complex global networks. For example, a firm can use electronic data interchange to assist communication with its supplier or join an electronic reverse auction marketplace and select the supplier with the lowest bids. Future research could enhance the generalisability of the framework by studying other forms of electronic mechanisms. The framework proposed in this paper sets foundation for future

empirical studies. We showed not including interactions may lead to substantially inferior results. Meanwhile, empirical studies can enhance the framework through validating the causalities proposed in this paper.

Acknowledgements

The authors are grateful to the editor and the anonymous reviewers for their constructive comments and suggestions.

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Note

- 1 The name of the company has been changed to protect its anonymity.